

Using letters instead of numbers

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

74	75
84	85

18	19
28	29

$\downarrow +10$
 $\curvearrowright +1$

n	$n+1$
$n+10$	$n+11$

$n-1$	n	$n+1$
$n+9$	$n+10$	$n+11$

n	$n+1$	$n+2$
$n+10$	$n+11$	$n+12$

$\leftarrow -1$ $\rightarrow +1$

$n-11$	$n-10$	$n-9$
$n-1$	n	$n+1$

$n-10$	$n-9$	$n-8$
n	$n+1$	$n+2$

$n-11$	$n-10$	$n-9$
$n-1$	n	$n+1$
$n+9$	$n+10$	$n+11$

$n-10$	$n-9$	$n-8$
n	$n+1$	$n+2$
$n+10$	$n+11$	$n+12$

Match the expression to its partner.

$a+a+a+a$

$a + 2+2$

$a \times a$

$4 + a + a$

$6+a-a-2$

$6a-4a$

$4 + a$

$4 + 2a$

$2a$

$4a$

a^2

4

This is part of a 1-100 number grid:

$n-21$		$n-10$		$n-9$
$n-1$				$n+1$
$n-20$		n		$n+2$
$n+20$	$n+9$		$n+11$	$n-2$
$n+10$	$n+22$	$n-22$		$n-11$

$$(3a)^2 = (3 \times 2)^2 \quad \text{Substitution}$$
$$= 36$$

If $a=2$ work out:

$$3a = 6$$

$$5a^2 = 5 \times 4$$
$$= 20$$

$$3a^2 = 3 \times 2^2$$
$$= 3 \times 4$$
$$= 12$$

$$5a - 3 =$$
$$10 - 3 = 7$$

$$10 - 2a = 6$$
$$10 - 4 = 6$$

$$\frac{a}{2} = 1$$

$$a^2 = 4$$

$$2a^3$$

Brackets

Indices (powers)

Division

Multiplication

Addition

Subtraction.

$$2 + 3 \times 5 = 2 + 15$$
$$= 17$$

1. $4 + 5 \times 2 = 14$

3. $5 \times 3^2 + 1 = 46$

2. $2 \times 4^2 = 32$

4. $4 + (2 + 1)^2 = 13$

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Substitution practice

If $a = 3$ evaluate

- 1) $5a =$
- 2) $6a - 4 =$
- 3) $2(a+5) =$
- 4) $a^2 =$
- 5) $a^3 =$
- 6) $2a^2 =$
- 7) $10 - a =$
- 8) $15 - 2a =$
- 9) $5(2a - 3) =$

If $a = 4$ evaluate:

- 10) $5a =$
- 11) $6a - 4 =$
- 12) $2(a+5) =$
- 13) $a^2 =$
- 14) $5a + 9 =$
- 15) $2a^2 =$
- 16) $10 - a =$
- 17) $15 - 2a =$
- 18) $5(2a - 3) =$
- 19) \sqrt{a}

If $a = 5$ and $b = 9$ evaluate

- 20) $2(a+b) =$
- 21) $b^2 =$
- 22) $a^3 =$
- 23) $2a^2 =$
- 24) $10 - a + b =$
- 25) $15 - 2a =$
- 26) $5(2a - b) =$
- 27) $2a - b$
- 28) $3b - 2a$
- 29) $\sqrt{b} =$

If $a = 1$ and $b = -2$ evaluate

- 30) $2(3a+b) =$
- 31) $a^2 =$
- 32) $a^3 =$
- 33) $b^2 =$
- 34) $10 - a + b =$
- 35) $15 - 2a =$
- 36) $5(2a - b) =$
- 37) $2a - b$
- 38) $3b - 2a$
- 39) $\sqrt{a} =$

Let $a=2$ and $b=3$. Work out:

$$5a + b = 13$$

$$5a + 3b = 19$$

$$ab = 6$$

$$9a - 3b = 9$$

$$3a^2 = 12$$

$$2a^2 + 5a = 18$$

13

1

12

If $b = 4$
write an expression with a
value of 20.

$$5b = 20$$

$$b^2 + 4 = 20$$

$$16 + b = 20$$

$$4b + 2 + 2 = 20$$

$$4b + b = 20$$

$$6b - 4 = 20$$

$$24 - b = 20$$

$$3b + 2b = 20$$

Simplifying expressions

$$\begin{aligned} \underline{a} + \underline{a} + \textcircled{b} + \textcircled{b} - \underline{a} &= 2b + 2a - a \\ &= 2b + a \end{aligned}$$

$$a - a + b + 3b = 4b$$

$$\cancel{x} + 3x - \cancel{x} + y + y = 3x + 2y$$

Algebra Pyramids

$$\begin{array}{c}
 \boxed{3a+3} \\
 \boxed{2a} \quad \boxed{a+3} \\
 \boxed{a} \quad \boxed{a} \quad \boxed{3}
 \end{array}$$

$$\begin{array}{c}
 \boxed{2b+a+3} \\
 \boxed{a+b} \quad \boxed{3+b} \\
 \boxed{a} \quad \boxed{b} \quad \boxed{3}
 \end{array}$$

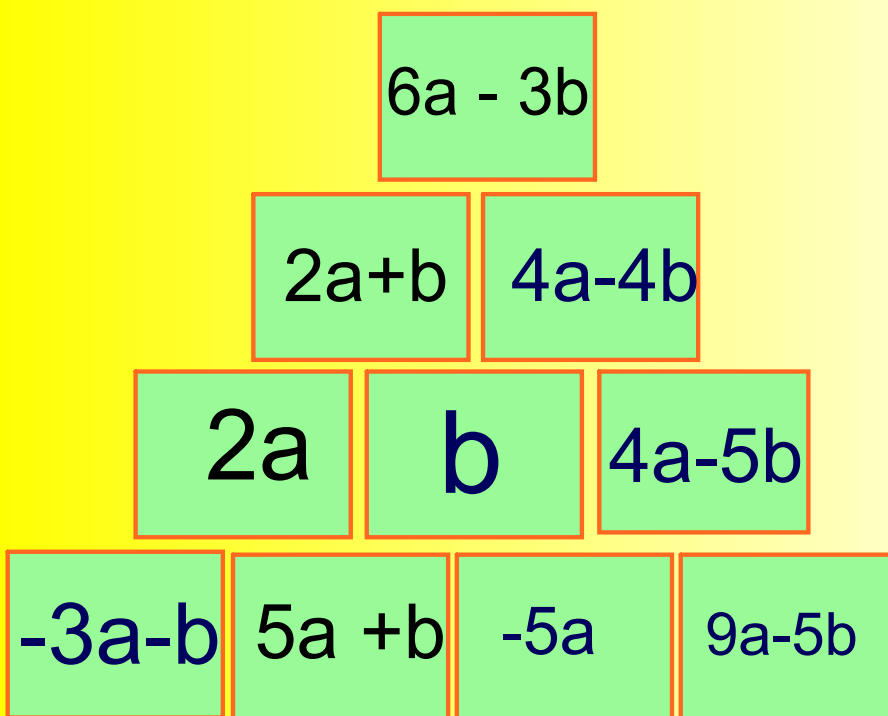
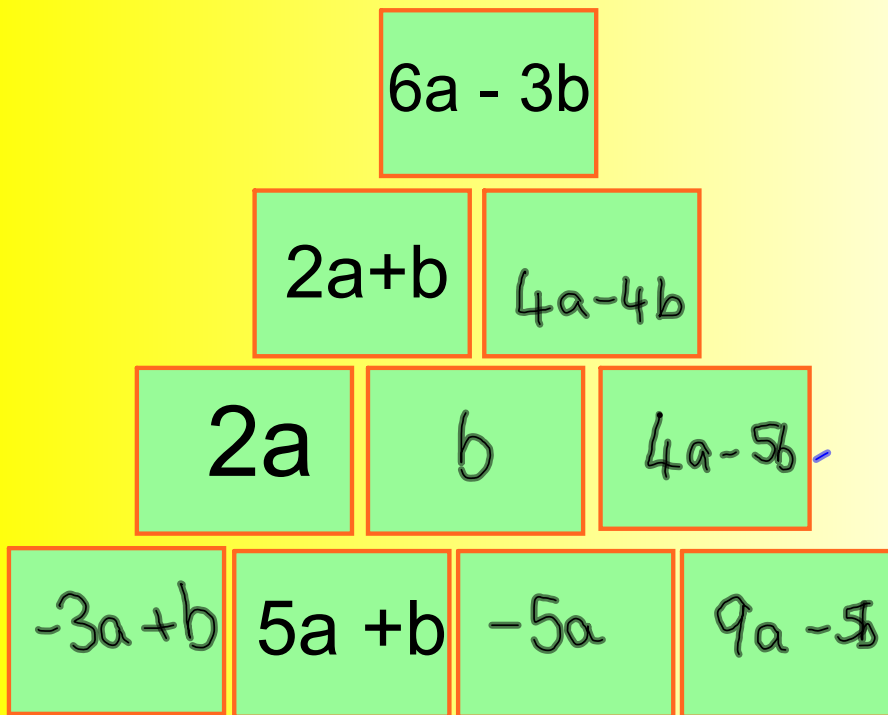
$$\begin{array}{c}
 \boxed{7a} \\
 \boxed{3a} \quad \boxed{4a} \\
 \boxed{2a} \quad \boxed{a} \quad \boxed{3a}
 \end{array}$$

$$\begin{array}{c}
 \boxed{6a+b+6} \\
 \boxed{2+3a} \quad \boxed{3a+b+4} \\
 \boxed{2} \quad \boxed{3a} \quad \boxed{b+4}
 \end{array}$$

$$\begin{array}{c}
 \boxed{5a+4} \\
 \boxed{3a} \quad \boxed{2a+4} \\
 \boxed{2a} \quad \boxed{a} \quad \boxed{a+4}
 \end{array}$$

$$\begin{array}{c}
 \boxed{9a} \\
 \boxed{5a} \quad \boxed{4a} \\
 \boxed{2a} \quad \boxed{3a} \quad \boxed{a}
 \end{array}$$

see worksheet
algebra pyramids



Make 6 rectangular cards

b	$b+2$	$b-2$
$2b$	b^2	$2b + 4$

$b=3$

$b=10$

$b=-4$

suppose I told you $2b = 10$...

what do I get if I add these two cards together

What if I doubled $b+2$...

Substitution

If $x=4$ work out:

$$\frac{x}{2} = 2$$

$$2x = 8$$

$$x+6 = 10$$

$$\sqrt{x} = 2$$

$$x-6 = -2$$

$$2x+3 = 11$$

$$x^2 = 16$$

Multiplying out Brackets

$$5(x+4) = 5x + 20$$

$$3(2a - 7) = 6a - 21$$

$$2(n+1) = 2n + 2$$

$$3(5n+1) = 15n + 3$$

$$5(n-6) = 5n - 30$$

$$10(3n+2) = 30n + 20$$

$$12(2n-3) = 24n - 36$$

$$2(3n+1) = 6n + 2$$

$$4(5n-2) = 20n - 8$$

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$$B1 \quad 2(x+4) = 2x + 8$$

Find the value of a

$$4+a = 7$$

$$a^2 = 36$$

$$2a+1 = 21$$

$$8-a = 3$$

$$a-10 = 5$$

Terminology

$2x$ TERM

$$5x+2=7x$$

$2x+5=4$ EQUATION

$$3x+8=16$$

$2x+y$ EXPRESSION

Simplify:

$$2x - x + y - 2y = x - y$$

$$4a - 5b + 3a - b = 7a - 6b$$

I am thinking of a number, add 5 to it, x by 2 and the answer is 16.

What was my number?

I am thinking of a number, add 10 to it, x by 3 and the answer is 45.

What was my number?

I am thinking of a number, x it by 4 and add 3. The answer is 11.

What was my number?

I am thinking of a number, subtract 7, x by 3 and the answer is 9.

What was my number?

Make up your own
"I'm thinking of a number".

Ask someone near you to solve it.

I'm thinking of a number sheet.

How many of these equations can you solve?

$$5x - 2 = 8$$

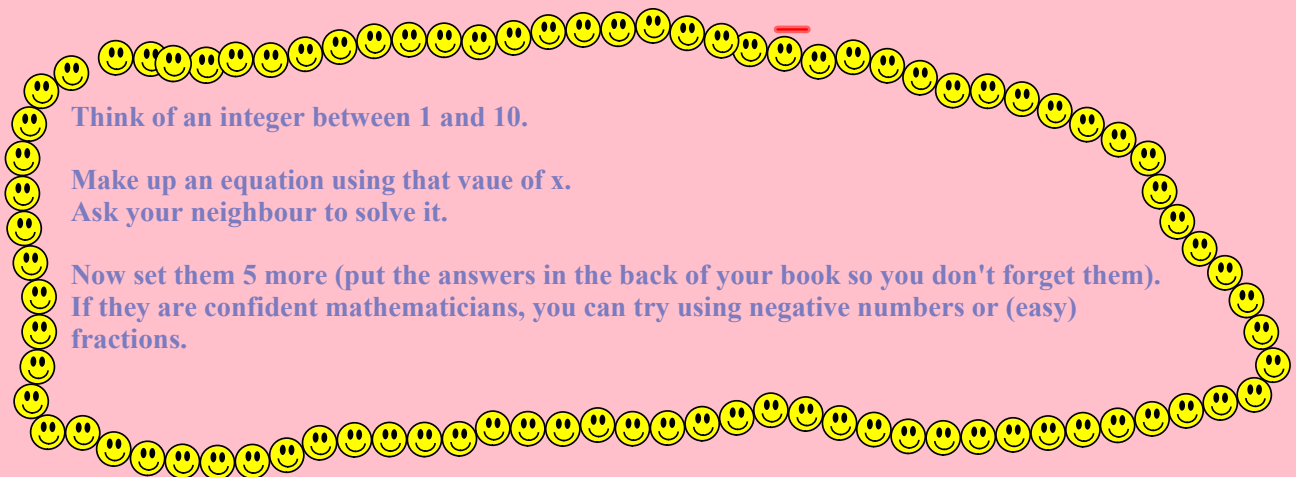
$$2x + 1 = 7$$

$$8 + 3x = 14$$

$$6 + 10x = 11$$

$$9 - x = 2$$

$$4x + 10 = -2$$

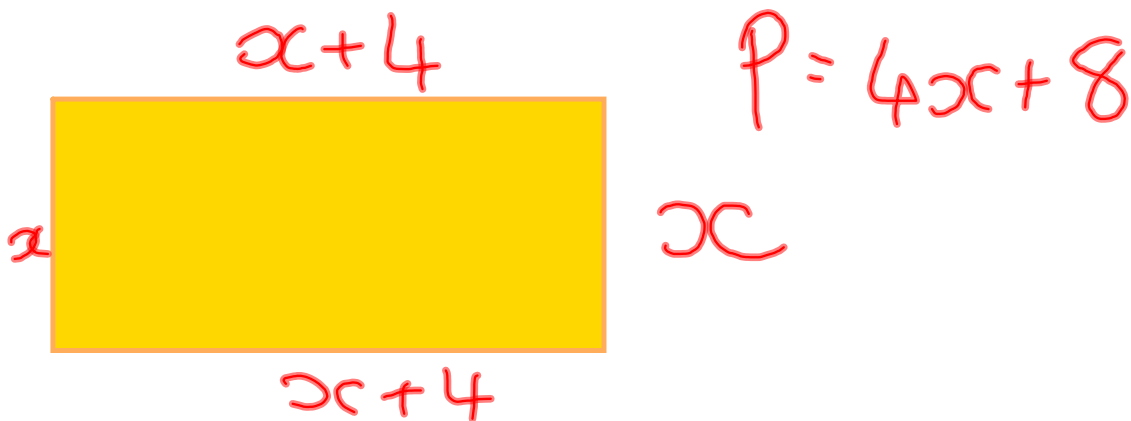


Think of an integer between 1 and 10.

Make up an equation using that value of x .
Ask your neighbour to solve it.

Now set them 5 more (put the answers in the back of your book so you don't forget them).
If they are confident mathematicians, you can try using negative numbers or (easy) fractions.

Forming Equations to solve problems



A rectangle has width x cm and the length is 4cm more than the width.

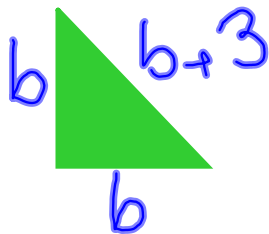
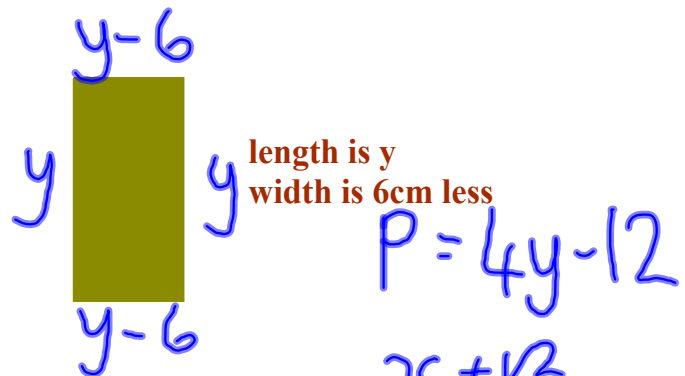
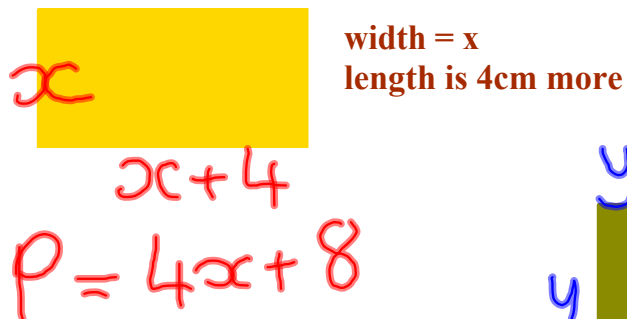
Write an expression for the perimeter.

If the perimeter is 48cm, find the length and width of the rectangle.

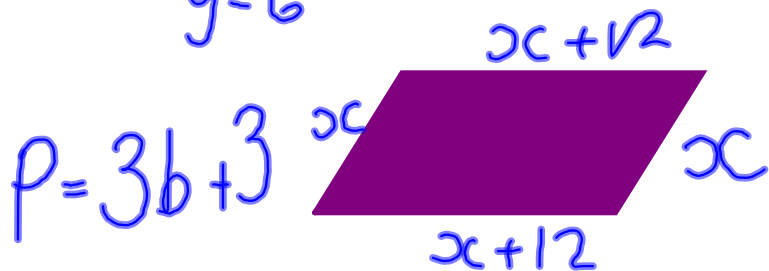
$$\begin{aligned} 4x + 8 &= 48 \\ 4x &= 40 \\ x &= 10 \end{aligned}$$

Forming expressions

Form an expression for the perimeter of each shape.



An isosceles triangle
two sides are b cm
the third side is 3 cm more



short side is x cm
long side is 12 cm more

$$P = 4x + 24$$

Making expressions

Jack has x pencils.
He lends out 3.
How many does he have now?



$$x - 3$$

Ben has n books.
He picks up another 4.
How many does he have altogether?

$$n + 4$$



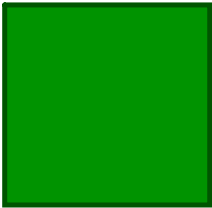
Holly has n scarves. n
Maria has twice as many $2n$
How many do they have altogether?



$$3n$$

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This square has side length x cm



1. Write down an expression for its perimeter.
2. Write down an expression for its area.
3. The area of the square is 36cm^2 .
 - a) Write down an equation to show its area.
 - b) Find the length of one side.
4. Find the perimeter of the square.

Using a spreadsheet to create number square

Task 1: a 1-100 square.

Open a new excel document.

Type 1 into cell A1

Type =A1+1 into cell B1,

find the cross, and drag across 9 squares.

Think about what you need to type into A2.

Remember to include the = sign.

Drag down.

Task 2: A 100-1 square

This time start with 100, and have the numbers descending.

Task 3: Create this number square:

2	4	6	8	10	12	14	16	18	20
22	24	26	28	30	32	34	36	38	40
42	44	46	48	50	52	54	56	58	60
62	64	66	68	70	72	74	76	78	80
82	84	86	88	90	92	94	96	98	100
102	104	106	108	110	112	114	116	118	120
122	124	126	128	130	132	134	136	138	140
142	144	146	148	150	152	154	156	158	160
162	164	166	168	170	172	174	176	178	180
182	184	186	188	190	192	194	196	198	200

The NC says you need to be able to:

- Begin to distinguish the different roles played by letter symbols in equations, formulae and functions; know the meanings of the words *formula* and *function*.
- Construct and solve linear equations with integer coefficients (unknown on either or both sides, without and with brackets) using appropriate methods (e.g. inverse operations, transforming both sides in the same way).
- Use formulae from mathematics and other subjects; **substitute integers into simple formulae**, including examples that lead to an equation to solve; derive simple formulae.

Attachments

Algebra pyramids.doc

Algebra pyramids answers.doc

I'm thinking of a number.doc

1-100 square.xls